Sub: Discrete Mathematics (MCA-100-22)

Date : 27/12/2023
Total Marks : 60
Time: 10.00 am To 12.30 pm

## Instruction:

. All questions are compulsory unless and otherwise stated.
2. Bold figures to the right of every question are the maximum marks for that question.
3. Candidates are advised to attempt questions in order.
4. Answers written illegibly are likely to be marked zero.
5. Use of scientific calculators, Log tables, Mollier Charts is allowed.
6. Draw neat and labelled diagram wherever necessary.

## Q. 1 Answer the following in 2-3 lines (Any 5)

1. If $f(x)=\frac{x^{2}+5 x-1}{2 x-1}$. Check whether the function even or odd?
2. Rewrite the following statement without using If-then:

If $b^{2}-4 a c=0$ then the roots of the quadratic equation are equal.
3. In a binomial distribution, find $p$ if mean $=5$ and variance $=5 / 2$.
4. If $p=\left(\begin{array}{lllll}1 & 2 & 3 & 4 & 5 \\ 5 & 1 & 3 & 2 & 4\end{array}\right), q=\left(\begin{array}{lllll}1 & 2 & 3 & 4 & 5 \\ 2 & 4 & 1 & 5 & 3\end{array}\right)$. Find: $p q \& q p$.
5. Write down the negation of the following statements:
(i) All equilateral triangles are equiangular.
(ii) Some parallelograms are rectangles.
6. If $f(x)=5 x-11$. Find $f^{-1}(2)$ and $f^{-1}(-3)$.
7. If X has a Poisson distribution with a parameter $\mathrm{m}=3$. Find $p(x \leq 1)$.

Given : $\left(e^{-3}=0.0497\right)$

## Q. 2 Answer the following in short. (Any 4)

1. A diet of a sick person must contain at least 400 units of vitamins, 60 units of minerals and 150 units of calories. Two foods F1 \& F2 are available at cost Rs. 10 anfd Rs. 15 per packet. If one unit of food F1 contains 200 units of vitamins, 1 unit of minerals and 50 calories whereas 1 of food F1 contains 300 units of vitamins, 3 unit of minerals and 60 calories. Formulate the problem as L.P.P. in order to meet the requirements of the sick person at minimum cost.
2. Show that: A group $G$ is abelian if and only if $(a b)^{2}=a^{2} \cdot b^{2} \forall a, b \in G$.
3. Identify the parameters: $f(x)=\frac{1}{\sqrt{10 \pi}} e^{\left(\frac{-x^{2}}{10}+4 x-40\right)},-\infty<x<\infty$
4. Solve the system of equations by Cramer`s Rule:
$2 x+5 y-4 z=12, x-y+2 z=3,-2 x+10 y+z=15$

Let $G$ be the group and $a, b \in G$. Then the equations $a x=b$ and $y a=b$ have unique solutions in G.
6. Find Expected value of ' $x$ ' for the following probability distribution:

| $x$ | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $P(x)$ | 0.12 | 0.27 | 0.21 | 0.31 | 0.09 |

## Q. 3 Answer the following in detail. (Any 3)

1. Prove : (i) Left cancellation law in groups. (ii) Right cancellation law in group.
2. A sample of 2000 electronic parts tested to find the length of life produced the following results: Mean, $\mu=12000$ hrs \& Standard Deviation , $\sigma=3000 \mathrm{hrs}$.
Assuming that the data are normally distributed, what percentage of electronic parts are expected to have a life (i) less than 6000 hrs. (ii) more than 15000 hrs (iii) in between 10000 to 14000

| Z | 0.67 | 1 | 2 |
| :--- | :--- | :--- | :--- |
| Area | 0.2487 | 0.3413 | 0.4772 | hrs.

The p.m.f. of a r.v. X is given by
3.

$$
\begin{aligned}
P(X=x) & =\frac{\binom{5}{x}}{32}, \quad x=0,1,2,3,4,5 \\
& =0 \quad, \quad \text { otherwise }
\end{aligned}
$$

Find: $P(x \leq 2)$ and $P(x \geq 3)$
Comment on the result.
4. A firm manufactures two types of dolls A and B . To produce a single unit of doll $\mathrm{A}, 10$ mins of cutting machine and 20 mins of polishing machine is required. To produce a single unit of doll B, 15 mins of cutting machine and 12 mins of polishing machine is required. Cutting machine is available for 4 hrs per day and polishing machine is available for 5 hrs per day. The profits on doll A and B are Rs. 50 and Rs. 60 respectively per piece. Only formulate the problem as L.P.P. in order to maximize the profit and solve it graphically.

